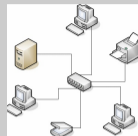


# NETWORKS

# Networks

- There are many types of networks and network effects
  - Physical: computers, railways
  - Social: online, family
  - Network externalities: value depends on # users
- Different fields, different (overlapping) refs, focus
- Economics is interested in
  - structure and dynamics of networks as graphs
  - implications of network externalities for firm strategy and market performance



# Network externalities

- Definition: *each consumer's valuation is increasing in the number of other consumers*
- Direct NE: telephones, email, languages
- Indirect NE: computer operating systems (software), automobiles (servicing); virtual networks
- Tariff-mediated NE: bank ATMs, cell phone plans



# The restaurant problem

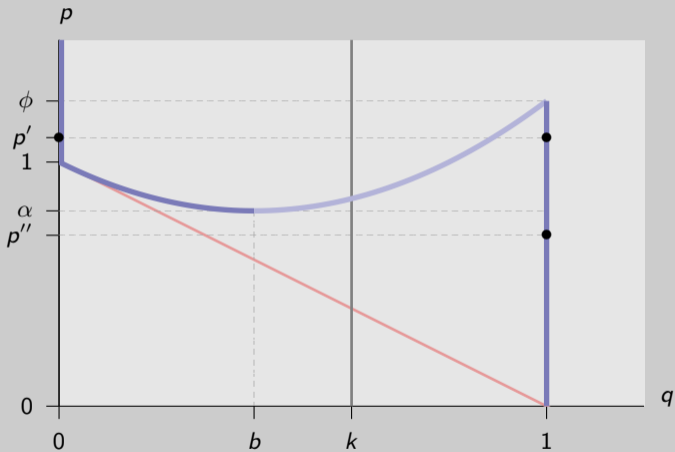
- Yogi Berra re Ruggeri's (a St. Louis restaurant):  
“Nobody goes there anymore; it's too crowded”
- Seriously, it should be either
  - Nobody wants to go there because it's always empty
  - Everybody wants to go there because it's always full of people
- Network effects may imply multiple fulfilled-expectations equilibria: some restaurants are “in”, some are “out”



# The restaurant problem

- consumer valuation:  $v = u + \phi e^2$ , where
  - $u$  uniformly distributed in  $[0,1]$
  - $e$ : expectation regarding # consumers
- If  $u'$  is lowest  $u$  who goes to restaurant,  $q = 1 - u'$  go.
- Fulfilled expectations:  $e = 1 - u'$
- Indifferent consumer:  $u' + \phi e^2 = p$ , or  $u' + \phi (1 - u')^2 = p$
- Since  $q = 1 - u'$ ,
$$p = 1 - q + \phi q^2$$
- Contrast  $\phi = 0$  with  $\phi > 0$

# The restaurant problem



# Fulfilled-expectations equilibrium

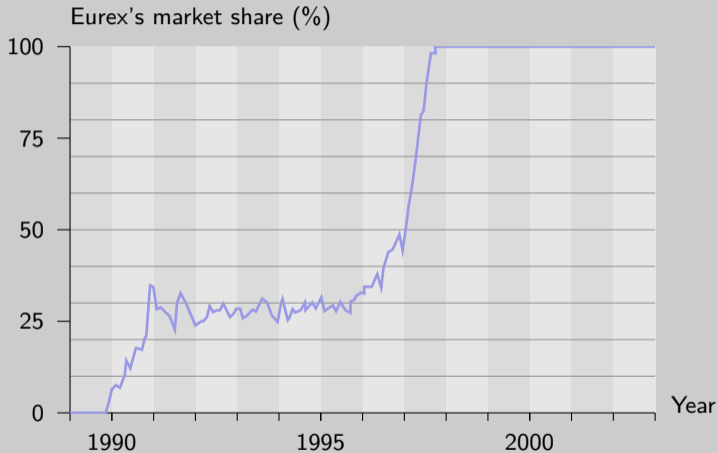
- Network effects may imply multiple demand levels for a given price
- Which value takes place depends on consumers' expectations regarding network size
- Unstable equilibria and tipping
- Pricing and capacity decisions with multiple equilibria

# The Battle of the Bund

- London International Financial Futures and Options Exchange (LIFFE): derivatives exchange est. 1982
- Items traded include future contracts on the Bund (German government bonds)
- Deutsche Terminbörse (DTB): based in Frankfurt, established January 1990; also trades Bund contracts
- Liquidity creates net effects, favors LIFFE (70% share)
- DTB follows aggressive strategy; market share gradually increases
- Once “tipping point” is crossed, DTB snowballs into monopoly

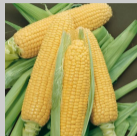


# The Battle of the Bund



# Theories of innovation adoption

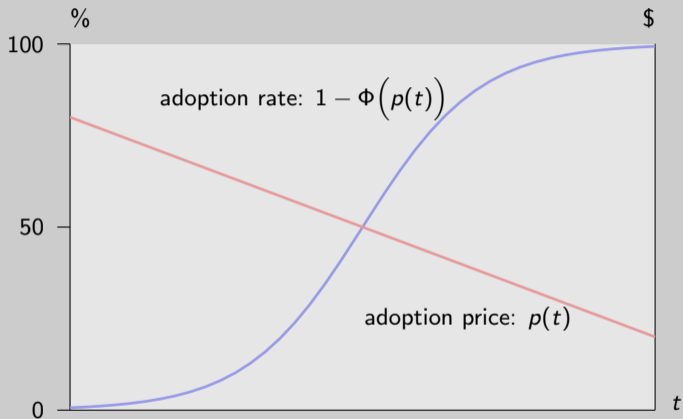
- Most innovations follow an S-shaped path
- Theory 1 (**diffusion**): agent heterogeneity
  - High valuation users go first; S curve from cdf
  - Example: hybrid corn
- Theory 2 (**epidemic**): word of mouth, social networks
  - matching informed, uninformed users; logistic S
  - Example: Google mail
- Theory 3 (**catastrophe**): networks externalities
  - value increasing in # other users; S from discontinuity
  - Example: fax machines



# Innovation diffusion

- Benefit from adoption:  $u \sim \Phi(u)$
- Cost from adoption:  $p(t)$
- Adoption by time  $t$ :  $x(t) = 1 - \Phi(p(t))$
- As  $p(t)$  declines, additional users adopt innovation
- If  $p(t)$  is approximately linear, then  $x(t)$  follows an S-shaped path — just like  $\Phi(\cdot)$

# Adopter heterogeneity and innovation diffusion



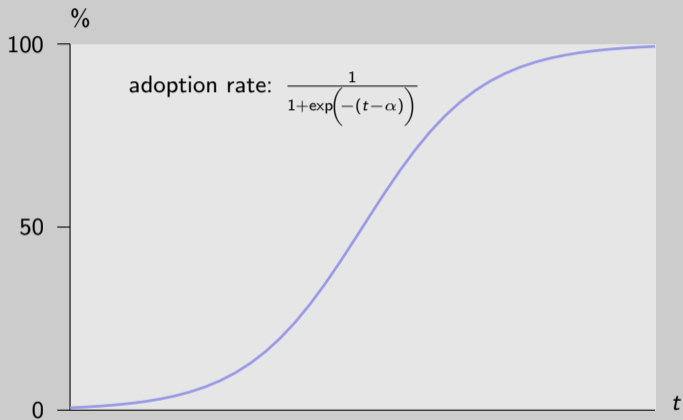
# Word of mouth and innovation adoption

- Gmail is available but very few potential users know about it: at time  $t_0$ , a fraction  $x_0$
- Each period, two email users meet
  - (a) one know Gmail, the other does not: new “convert” to Gmail
  - (b) neither knows about Gmail: nothing happens
  - (c) both know Gmail account: nothing happens
- This implies

$$x_t = \frac{1}{1 + \exp(-(t - \alpha))}$$

where  $\alpha = t_0 + \ln(1 - x_0) - \ln(x_0)$

# Word of mouth and innovation diffusion



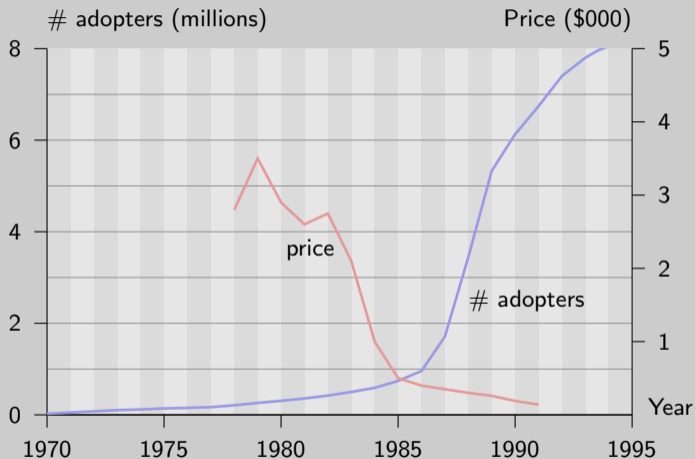
# Technology adoption as a coordination game

- It's only worth having a fax machine if others have a fax machine too (before Internet)
- In game theory terms, this is equivalent to the coordination game

		Player 2	
		Old	New
Player 1	Old	1 1	0 0
	New	0 0	2 2

- Strong network externalities imply multiple equilibria

# Adoption of fax machines in US



# Innovation adoption with network effects

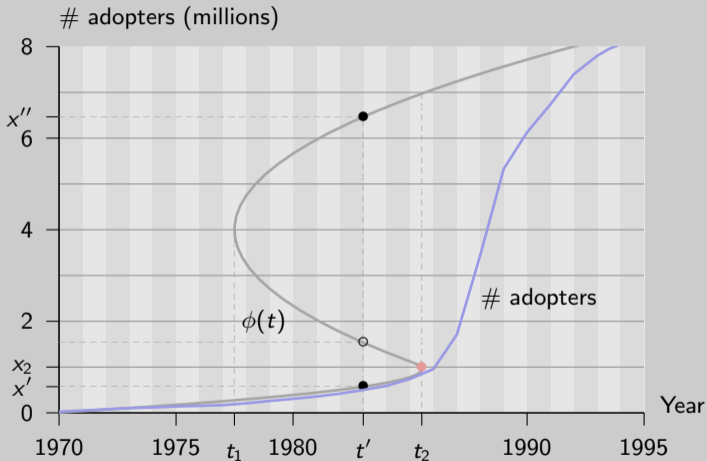
- Adoption benefit:  $u + \psi(x)$
- $u \sim$  cdf  $\Phi(u)$
- $p(t)$ : adoption price
- $A$ : # potential adopters
- $x(t)$ : # actual adopters at time  $t$
- $u'$ : indifferent adopter's value of  $u$ ; all with  $u > u'$  adopt

$$u' + \psi(x(t)) = p(t)$$

$$x(t) = A(1 - \Phi(u'))$$

- $\phi(t)$ : equilibrium values of  $x$  at time  $t$

# Adoption of fax machines in US



## Fax machines in US: summary

- From about 1980 to about 1987, there are two fulfilled-expectations equilibria (chicken and egg)
- If expectations are given by latest observation, then up to about 1987 industry follows low equilibrium
- At about 1987, a critical mass (tipping point) is achieved
- For a brief period of time, system in disequilibrium (snow-ball): buyer expectations exceeded
- New, higher adoption equilibrium is eventually reached

# Inertia and tipping

- Consider a new product or technology: will it be adopted too quickly or too slowly?
- Excess inertia: nobody buys it because nobody buys it (multiple equilibria)
- Excess momentum: market tips very quickly towards new product even when it does not represent a great improvement



## Excess inertia

- Users 1 and 2 simultaneous choose old or new version
- Old version worth  $a_i$  ( $i = 1, 2$ ), New version worth  $b_i$
- Switch from Old to New costs  $c_i$
- Network effects: each version useless unless other player chooses same version

## Excess inertia

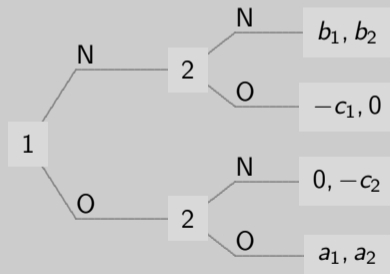
		User 2	
		$O$	$N$
User 1	$O$	$a_1$ $a_2$	$0$ $-c_2$
	$N$	$-c_1$ $0$	$b_2 - c_2$ $b_1 - c_1$

## Excess inertia

- $b_i - c_i > a_i \Rightarrow (N, N)$  eq'm Pareto dominates  $(O, O)$  eq'm
- Suppose  $b_i = 2c_i$  and that  $c_i$  is very large
- Switching from  $O$  to  $N$  = "lottery" yielding  $-c_i$  or  $+c_i$   
(depending on other player's choice)
- Reasonable to assume  $(O, O)$  eq'm will play out

## Excess momentum

- Sequential game;  $b_1 \gtrsim a_1$ ;  $b_2 \gtrsim 0$
- Subgame perfect eq'm: choose version  $b$
- Since  $b_1 \approx a_1$  and  $b_2 \approx 0$ ,  $b_1 + b_2 < a_1 + a_2$



# Excess momentum

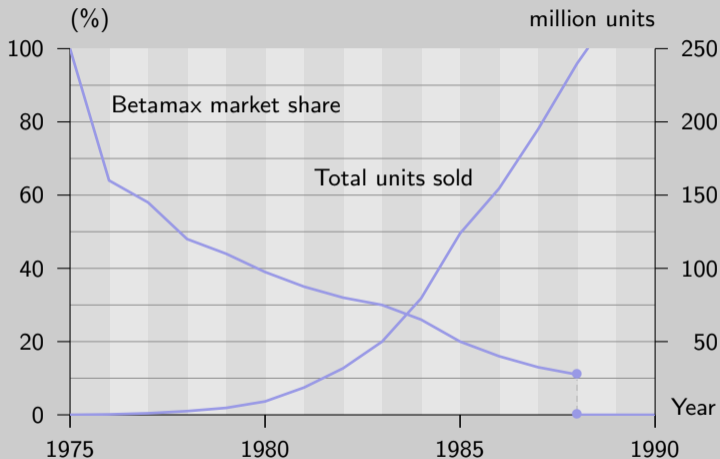
- Equilibrium: both switch to new technology
- Total payoff before switch =  $2 v_0$
- Total payoff after switch  $\approx v_0$
- Intuition:
  - Lead adopter has small benefit, imposes huge loss on second adopter
  - Second adopter is better off with new technology *given that* first adopter adopts new technology
- Terminology: bandwagon effect, domino effect, snow-ball effect

# Inertia and tipping

- Consider a new product or technology: will it be adopted too quickly or too slowly?
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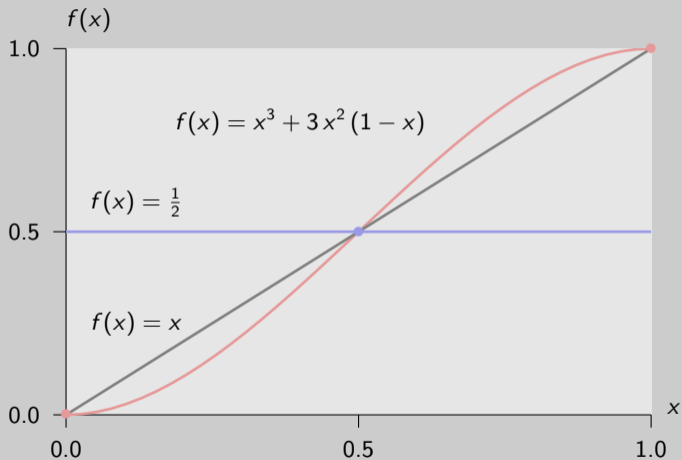
# VHS v Betamax



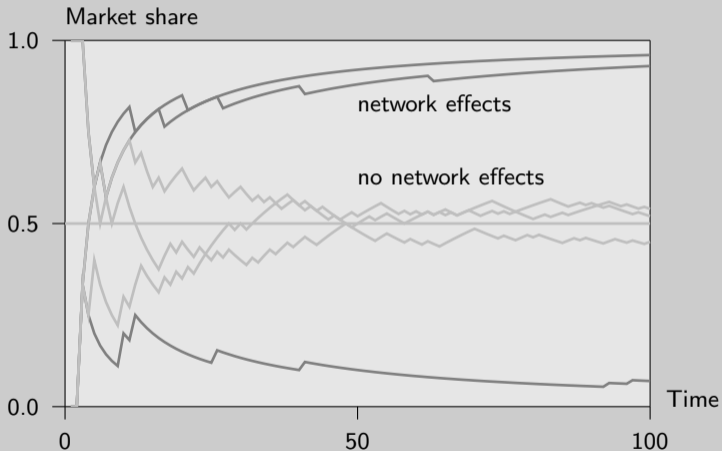
# Standards wars

- Two versions of a new technology: blue and red
- Adopters arrive sequentially
  - No network effects: flip a coin
  - Network effects: poll 3 of the past adopters; follow majority
- What happens to the fraction  $x(t)$  of blue adopters?
- Theorem: converges almost surely to a stable fixed point of  $f(x)$ , the probability next ball is blue given current fraction of blue balls

# Adoption probability

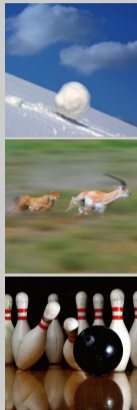


# Standards wars

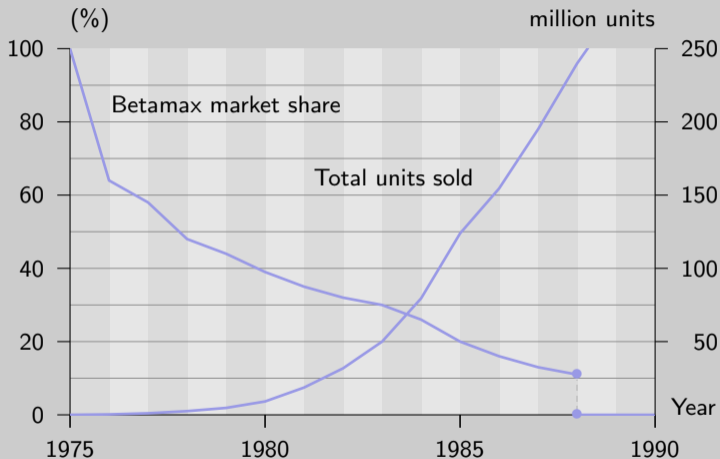


# Standards wars

- Eventually, one design takes over the entire market, while the other is “orphaned:” self-reinforcing dynamics, snow-ball effects.
- The winning technology is not necessarily the best or the one preferred by most consumers; the fittest does not necessarily survive.
- The ultimate outcome of the battle depends on a series of “small historical events;” the outcome is path dependent.

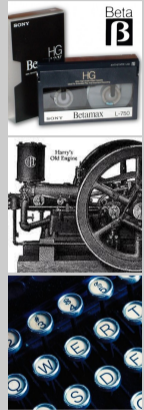


# VHS v Betamax



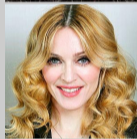
# Examples

- Videocassette recorder
- gasoline engine
- QWERTY keyboard
- NB: interpretation of these examples highly controversial



# Viral processes and superstars

- Vanishing middle: feature of the “new economy”
- Improved search cheaper production: embarrassment of niches (a.k.a. the long tail)
- At opposite end: supermegablockbusters: combination of social networks, globalization
  - Media (music, movies, books, newspapers)
  - Some professions (CEOs, medicine)
- How do superstars emerge?



# Network externalities and social networks

- So far, assumed very simple network structure: each user is equally likely to connect to any other user
- In practice, networks has very specific structure
- Example #1: video game standards have different shares of different demographics
- Exmample #2: diffusion of Facebook shows that it's not just # users that matters



# Takeaways

- Network effects crop up everywhere; they can lead to excess inertia, and may allow small seemingly random events to influence ultimate outcome